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# Optimal Dynamic Fisheries Enforcement

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# Introduction

Fisheries management consists of:

- (i) A fisheries management system (a set of rules)
- (ii) The enforcement of these rules

Within a given fisheries management system

**The actual fisheries management is  
fisheries enforcement!!**

So, a sensible fisheries policy needs to pay great attention to fisheries enforcement

# Basic enforcement model

Private benefits of fishing:  $B(q,x)$

Social benefits of fishing:  $B(q,x) + \lambda \cdot (G(x) - q)$

Shadow value  
of biomass

## The Enforcement Sector:

Enforcement effort:  $e$  — Endogenous  
(control)

Cost of enforcement:  $C(e)$

Penalty level:  $f$  — Exogenous

Announced target:  $q^*$  — Exogenous

# The penalty function

$$F(f, q - q^*)$$

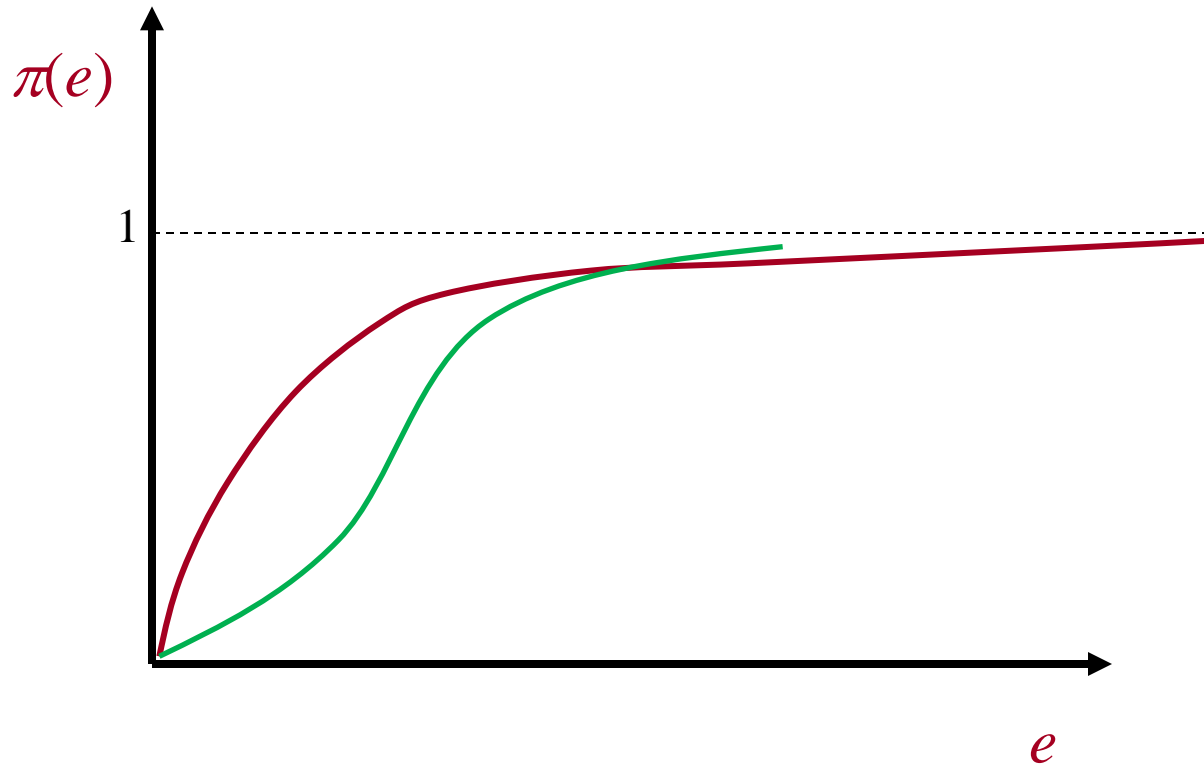
$$F(f, q - q^*) \geq 0,$$

$$F(0, q - q^*) = F(f, 0) = 0,$$

$$F_f \geq 0, F_2 \geq 0$$

# Model (cont.)

Probability of penalty function (if violate):  $\pi(e)$



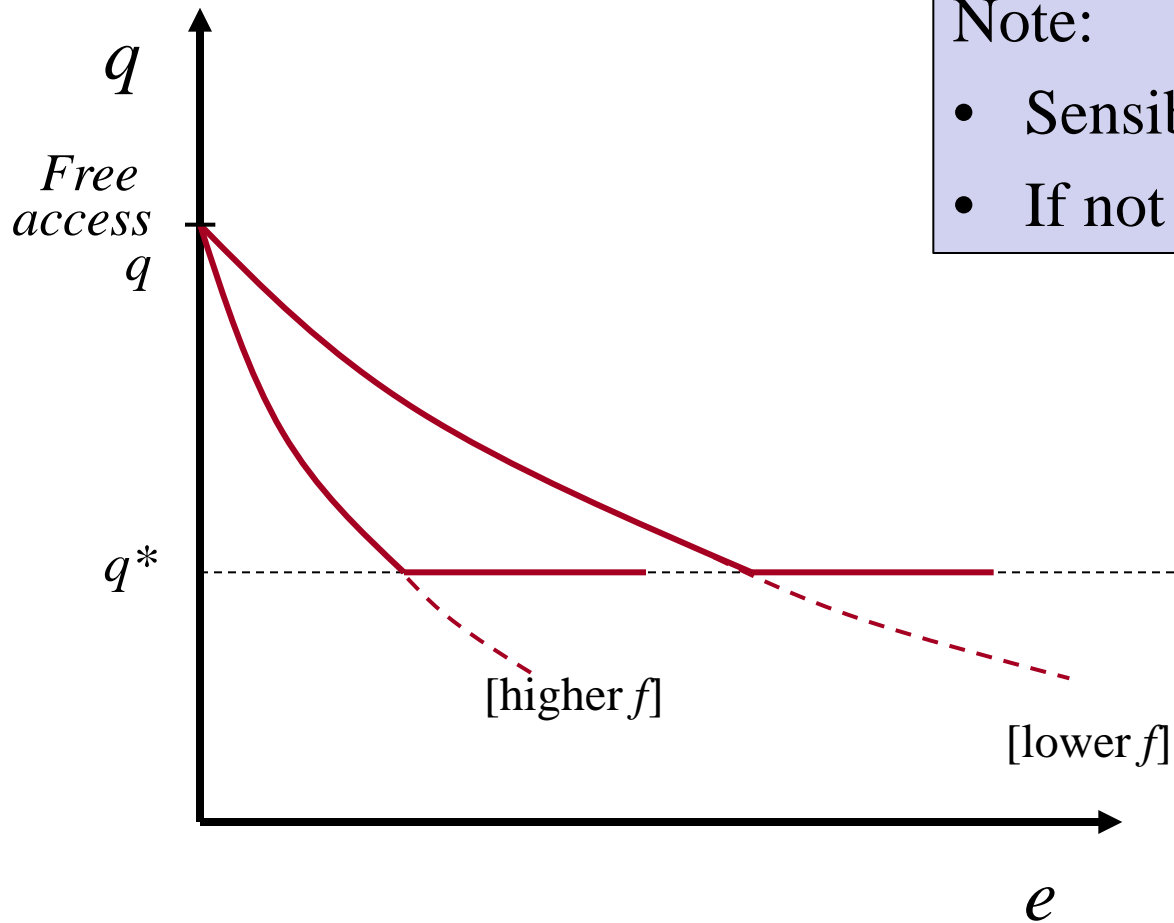
# Private behaviour

Maximization problem:  $Max B(q,x) - \pi(e) \cdot F(f, q - q^*)$

Necessary condition:  $B_q(q,x) - \pi(e) \cdot F_2 = 0$

$\Rightarrow$  Enforcement response function:  $q = Q(e, x, f, q^*)$

# Enforcement response function



Note:

- Sensible  $q > q^*$
- If not  $\Rightarrow$  trouble

# Socially optimal enforcement

The optimality problem

$$\underset{e}{\text{Max}} B(q,x) + \lambda \cdot (q - G(x)) - C(e).$$

Subject to:  $q = Q(e, x; f, q^*)$ , ..etc.

⇒ Basic enforcement rule

$$(B_q - \lambda) = \frac{C_e}{Q_e} = \frac{\partial C}{\partial q} < 0$$



# Some implications

1. Traditional optimality condition:  $B_q = \lambda$ .

Optimality with costly enforcement:  $B_q < \lambda$

$\Rightarrow q_{opt} > q^o$  (traditional optimality ignoring enforcement)

2.  $q_{opt} > q^*$  ( $q^*$  is the announced *TAC*)

$\Rightarrow q^*$  is not the real target (for show only).

Noncompliance is the desired outcome!

3. Ignoring enforcement costs can be very costly

i. Wrong target harvest

ii. Inefficient enforcement

# Practical applications of the theory: Enforcement agency needs to know

1. The private benefit function of fishing,  $B(q,x)$
2. The shadow value of biomass,  $\lambda$
3. The enforcement cost function,  $C(e)$
4. The penalty function,  $\pi(e)$
5. The penalty structure,  $f$

Note: Items 1 & 2 come out of a bio-economic model of the fishery.

Items 3, 4 and 5 are special enforcement data

# Why dynamics?

- This theory is fine for the enforcement agency
  - Only needs to be informed of the current  $\lambda$
- However,  $\lambda$  depends on future  $x$  (which depends on current enforcement)
- So,  $\lambda$  is endogenous!!
- Also, for longer term enforcement planning need the dynamic context

# Optimal dynamic enforcement

$$\mathit{Max}_{\{e\}} V = \int_0^{\infty} [B(Q(e, x; f), x) - C(e)] \cdot e^{-r \cdot t} dt$$

*Subject to*  $\dot{x} = G(x) - Q(e, x; f, q^*), \dots \text{etc.}$

# Necessary conditions

$$(1) (B_q(q, x) - \lambda) \cdot Q_e(e, x; f, q^*) = C_e(e), \quad \forall t$$

$$(2) \dot{\lambda} - r \cdot \lambda = -B_q(q, x) \cdot Q_x(e, x; f, q^*) - B_x(q, x) \\ - \lambda \cdot (G(x) - Q_x(e, x; f, q^*)), \quad \forall t$$

$$(3) \dot{x} = G(x) - Q(e, x; f, q^*), \quad \forall t$$

(1) is the basic (static) social enforcement rule!!

(2) describes the optimal evolution of  $\lambda$

# Optimal equilibrium

Costly enforcement

$$\lambda = \frac{B_x + B_q \cdot Q_x}{r - G_x + Q_x}$$

$$G_x + \frac{C_e \cdot Q_x + B_x \cdot Q_e}{B_q \cdot Q_e - C_e} = r$$

No or costless enforcement

$$\lambda = \frac{B_x}{r - G_x}$$

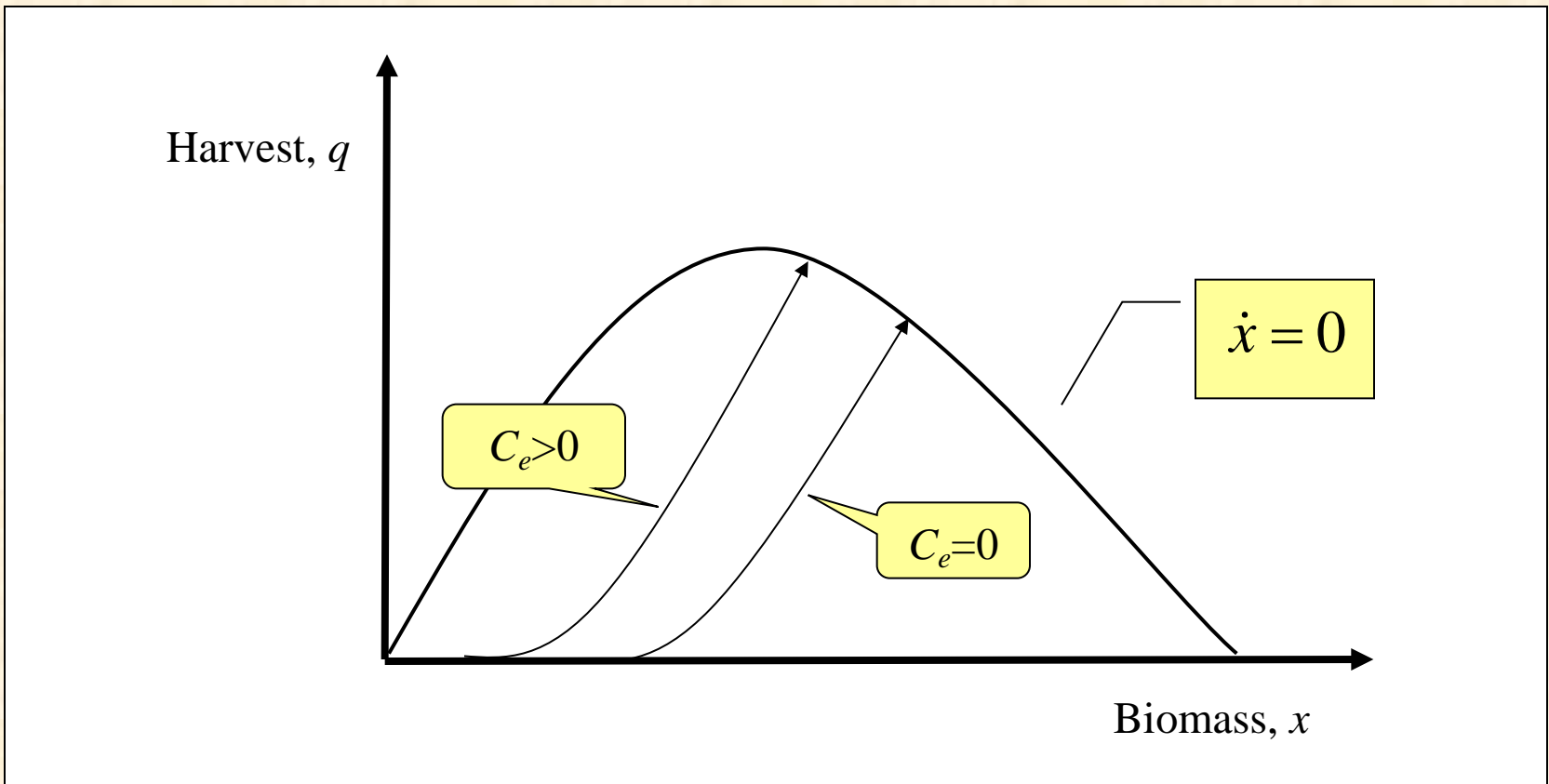
$$G_x + \frac{B_x}{B_q} = r$$

# So, enforcement modifies the marginal stock effect, $\Gamma$

- In traditional fisheries models,  $\Gamma > 0$
  - Under costly enforcement,  $\Gamma$  can be of any sign
  - However, likely that  $\frac{\partial \Gamma}{\partial C_e} < 0$
- ⇒ Thus  $\Gamma(\text{enforcement}) < \Gamma(\text{costless enforcement})$
- $x(\text{enforcement}) < x(\text{costless enforcement})$

# Optimal feed-back rules

Can show that  $q_{opt}(x) \geq q^{\circ}(x)$  !





# Numerical example

$$p \cdot q - c \cdot \frac{q^2}{x} - FK - f \cdot \pi(e) \cdot q$$

$$Q(e, x, f) = \frac{(p - f \cdot \pi(e)) \cdot x}{2 \cdot c}$$

$$\pi(e) = \frac{e}{\eta + e}$$

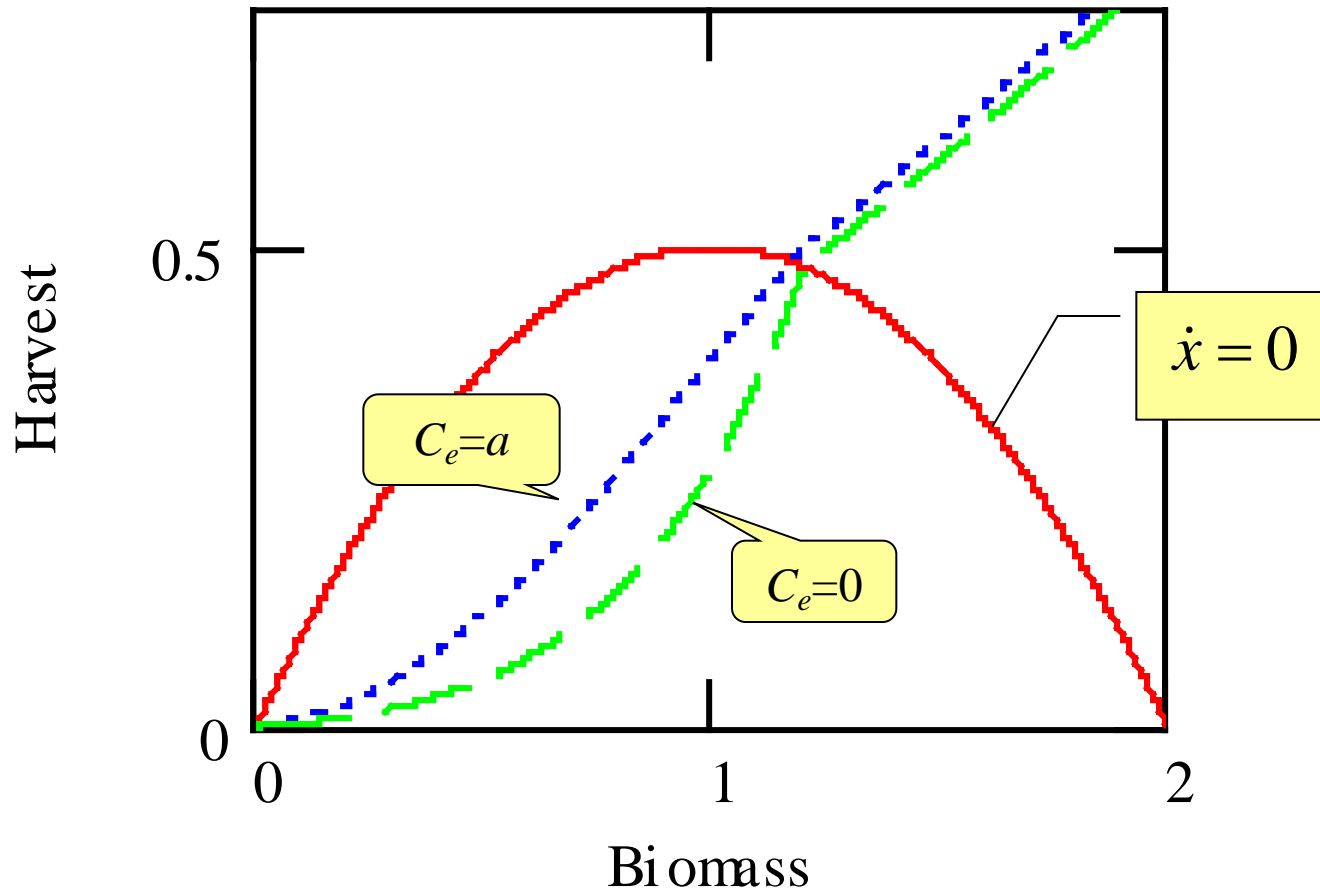
$$C(e) = a \cdot e$$

$$x_{t+1} = x_t + \alpha \cdot x_t - \beta \cdot x_t^2 - q_t$$

## Parameters

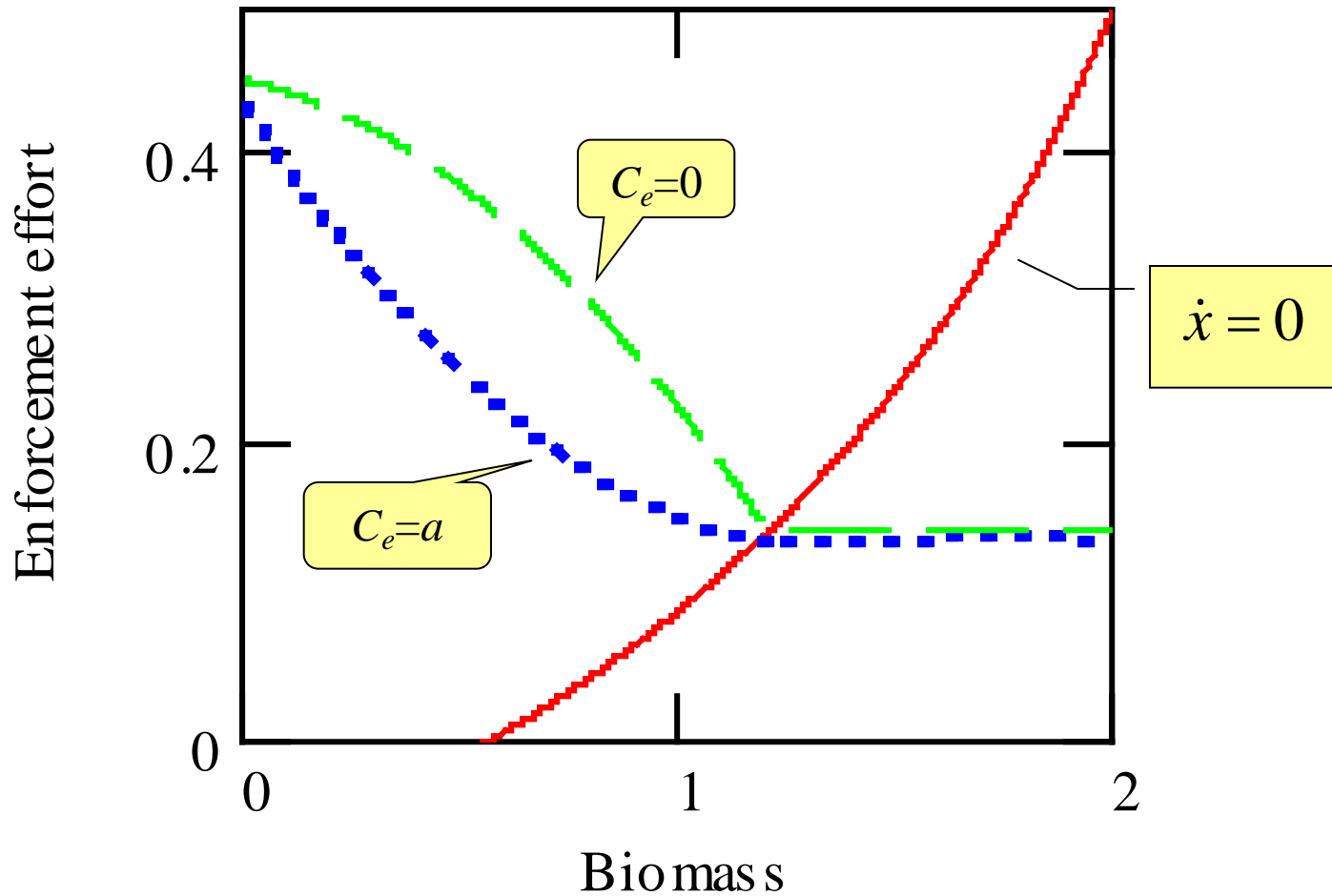
$\alpha$	1
$\beta$	0.5
$p$	1
$f$	2
$a$	0.1
$\eta$	0.5
$c$	0.7
$r$	0.05
$FK$	0.1

# Optimal Paths (harvest-biomass space)



# Optimal Paths

(enforcement effort-biomass space)



# Note

- Optimal enforcement depends on biomass
  - Important practical implications for set-up and operations of enforcement agencies
- Optimal enforcement is high at low biomass levels (high  $\lambda$ ) and vice versa
- High enforcement costs may render enforcement and, therefore, fisheries management uneconomical

# Enforcement by adjusting $f$ or $q^*$

- Can probably adjust  $f$  and  $q^*$  at no or very low cost

⇒ Economically preferable

- If enforcement is costless ⇒  $q_{opt} = q^\circ(x)$

In that case optimal feed-back rules for  $f$  and  $q^*$  are implicitly defined by

$$q^\circ(x) = Q(e, x; f, q^*).$$

# Can show

$$\frac{\partial f}{\partial x} < 0$$

$$\frac{\partial q^*}{\partial x} > 0$$

$$q^*(x) < q_{opt}(x)$$

**END**

# Numerical results

## The whole program

Present value of program (social): 4.145

Private value of program: 0.553

Private and social value of no enforcement: 2.409

Present value of fines: 3.878

Present value of enforcement costs: 0.286



# Numerical results

## Equilibrium

Social benefits: 0.242

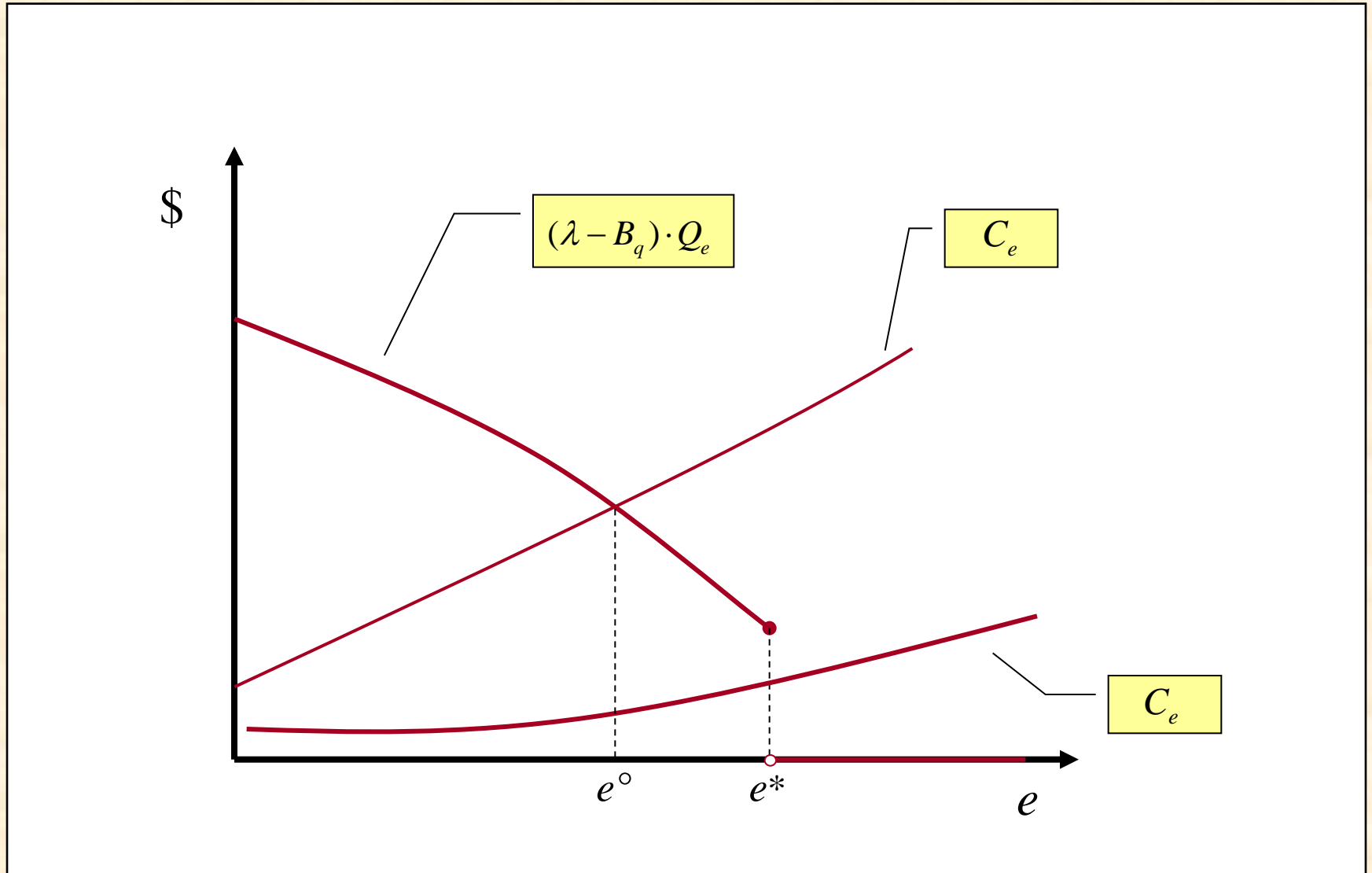
Private benefits: 0.046

Fines: 0.210

Enforcement costs: 0.013

Enforcement costs/revenues: 0.026

# Social optimality: Illustration



# To apply theory: Empirical requirements

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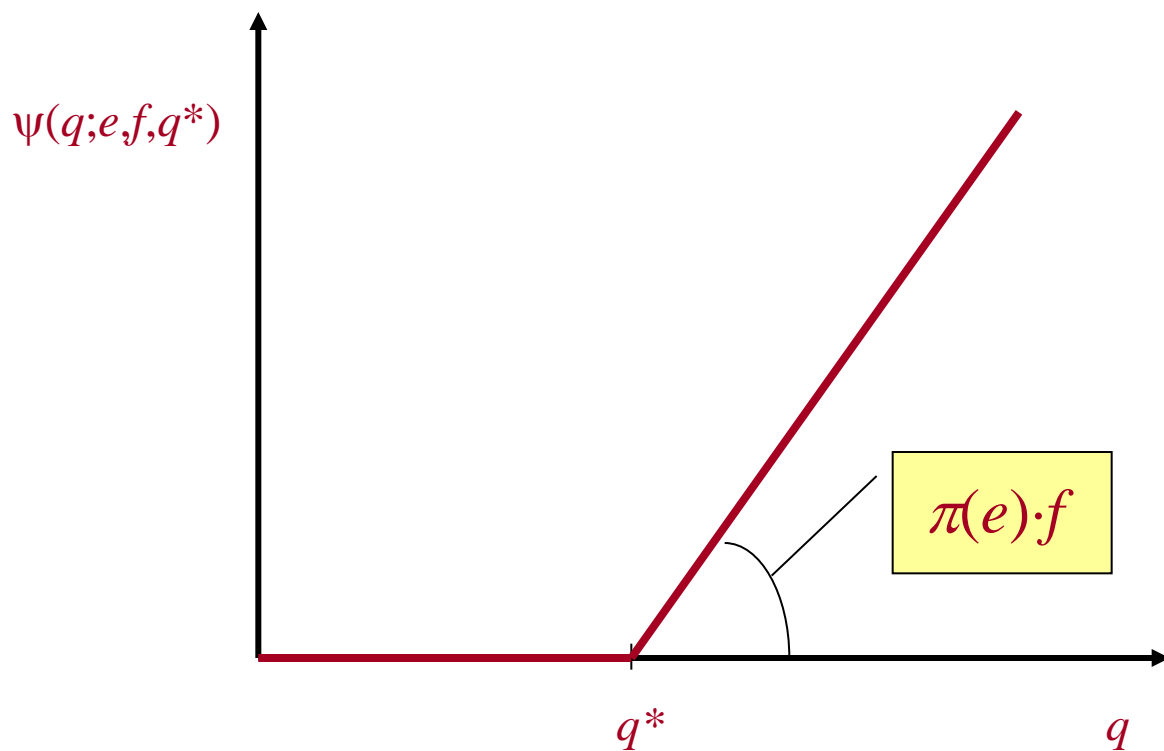
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# Model (cont.)

Private costs of violations:  $\psi(q;e,f,q^*)=\pi(e)\cdot f\cdot(q-q^*)$ , if  $q\geq q^*$

$\psi(q;e,f,q^*) = 0$  , if  $q < q^*$



# Model (cont.)

Private benefits under enforcement

$$B(q,x) - \pi(e) \cdot f \cdot (q - q^*), \quad q \geq q^*$$

$$B(q,x), \text{ otherwise}$$

Social benefits with costly enforcement:

$$B(q,x) - \lambda \cdot q - C(e)$$

# The discontinuity problem

- Analytically merely cumbersome
- Practically troublesome
  - Stop getting responses to enforcement alterations
- To avoid the problem
  - Set  $q^*$  low enough (lower than the real target)
  - Aim for the appropriate level of noncompliance
- A well chosen  $q^*$  is not supposed to be reached ( $\Rightarrow$  Non-compliance is a good sign!)